

# Electronic Structure of Tetrahedral Iron(III)–Sulfur Clusters in Alkaline Thioferrates: An X-Ray Absorption Study

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X-ray absorption spectra of  $\text{Na}_5\text{FeS}_4$  and  $\text{KFeS}_2$  containing separate and interconnected edge-shared  $\text{FeS}_4^{3-}$  tetrahedra, respectively, are reported and interpreted in terms of an  $S = 5/2$  ground state for  $\text{Fe}^{3+}$  in both compounds. A rather small value of the ligand-to-metal charge transfer energy  $\Delta_{\text{eff}}$  was indicated by the comparison of the experimental Fe 2p XAS spectrum with atomic multiplet calculations, reflecting an almost 1 : 1 admixture of  $d^5$  and  $d^6L$  ( $L$  hole on the ligand) character in the ground state for  $\text{Na}_5\text{FeS}_4$ . The broadening of the main peak toward higher energies when going from  $\text{Na}_5\text{FeS}_4$  to  $\text{KFeS}_2$  is attributed to symmetry lowering from  $T_d$  to  $D_{2d}$ . Ligand-field parameterization schemes, such as the angular overlap model, are found to be quantitatively not applicable for the systems under consideration. The phase diagram of  $d^5$  ions and its dependence on the crystal-field splitting (10Dq) and the ligand-to-metal charge transfer energy ( $\Delta_{\text{eff}}$ ) are discussed and it is shown that an intermediate spin state ( $S = 3/2$ ) can become stable for negative  $\Delta_{\text{eff}}$  and moderate values of 10Dq and metal–ligand hybridization. This presents another limit for the ligand-field approach and the Tanabe–Sugano diagrams, where only  $S = 5/2$  and  $S = 1/2$  ground states are predicted. For the  $\text{Fe}^{3+}$  in a tetrahedral field the theory indicates that it is unlikely that the  $S = 3/2$  and  $S = 1/2$  states become the ground state since the gain in energy due to ligand–ligand coupling and the relatively small charge transfer energy (both tending to lower energetically the  $S = 3/2$  state) are not sufficient to overcome the high exchange stabilization of the high-spin ( $S = 5/2$ ) state. © 1995 Academic Press, Inc.

## I. INTRODUCTION

Alkaline iron(III) chalcogenides  $A_x\text{Fe}_yX_z$  ( $A = \text{K}, \text{Rb}, \text{Cs}$ ;  $X = \text{S}, \text{Se}, \text{Te}$ ) containing tetrahedral  $\text{FeS}_4^{3-}$  units have been the subject of a long-standing controversy regarding their electronic structure and ground state spin multiplicity. Varying the content ( $x$ ) of the alkaline ion, it was possible to synthesize ionic lattices with separated  $\text{FeS}_4^{3-}$  tetrahedra (in  $\text{Na}_5\text{FeS}_4$  (1)), dimeric units consisting of bitetrahedra sharing common edges ( $\text{Fe}_2\text{S}_6^{6-}$  in  $\text{Na}_3\text{FeS}_3$  (2)), and linear chains with  $[\text{FeS}_2]^-$  units and  $\text{FeS}_4^{3-}$  tetrahedra slightly elongated along the pseudo- $S_4$ -axis, extending in one dimension (in  $A\text{FeS}_2$ ,  $A = \text{K}, \text{Rb}, \text{Cs}$  (3a, 3b)). In addition,  $\text{CsGaS}_2$  with the same structures as  $\text{KFeS}_2$  and  $\text{RbFeS}_2$  was used as a host material in which  $\text{Ga}^{3+}$  was substituted with  $\text{Fe}^{3+}$  up to 25% without changing the crystal structure (4). Structural views for  $\text{Na}_5\text{FeS}_4$  and  $\text{KFeS}_2$ , adopted from references (1) and (3b), respectively, are shown in Fig. 1.

Magnetic, optical, and neutron diffraction experiments, together with Mössbauer data on these systems, offer the unique possibility of following experimentally the cooperative effects that evolve in going from separate coordination units  $\text{FeS}_4^{3-}$ , to dimers, to one-dimensional chains. Fe(III) is a  $d^5$  ion and according to ligand field theory, in a cubic field it can assume either a high-spin,  $S = 5/2$ ,  $e^2t_2^3$  configuration or a low-spin,  $S = 1/2$ ,  $e^4t_2^1$  configuration. In tetrahedral coordination with an  $e < t_2$  splitting pattern and a 10Dq which is 4/9 from the octahedral value, it is expected that a high-spin ( $S = 5/2$ ) state will be stabilized, although one should realize that the interatomic distances are smaller for the tetrahedral site, increasing the 10Dq value slightly. In line with this, magnetic measurements at temperatures higher than the Néel point ( $T_N = 28\text{K}$ ) show

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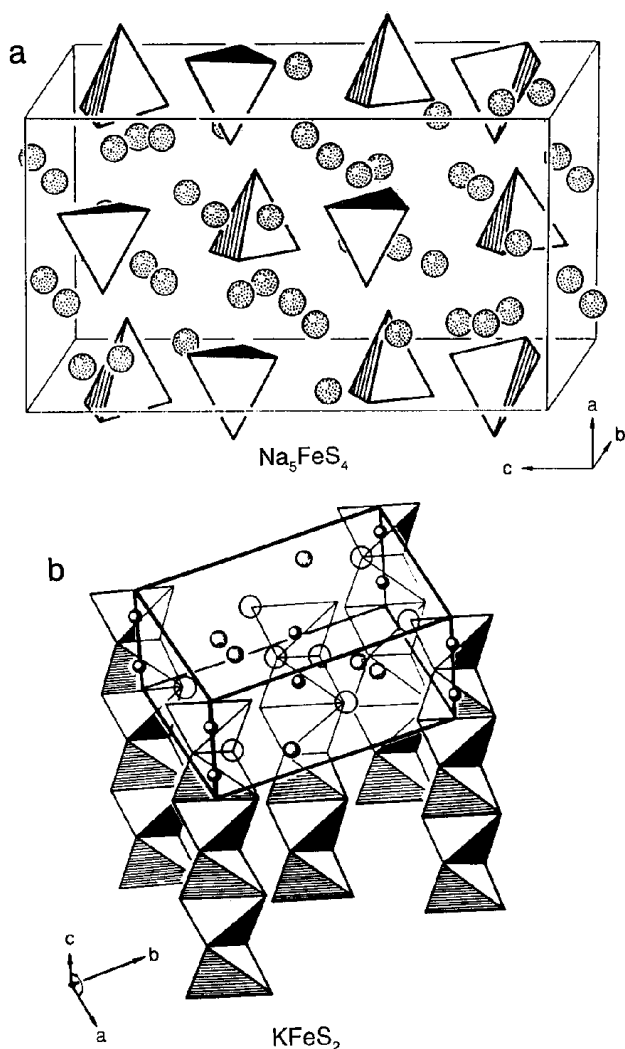


FIG. 1. Tetrahedral framework structures: (a) isolated tetrahedra in  $\text{Na}_5\text{FeS}_4$  (adopted from Ref. (1)); (b) chains of edge-sharing tetrahedra in  $\text{KFeS}_2$  (adopted from Ref. (3b)).

Curie-Weiss behavior for  $\text{Na}_5\text{FeS}_4$  with an effective magnetic moment of  $5.6 \mu_B$ , indicating five unpaired electrons on iron ( $S = 5/2$  spin only value,  $5.96 \mu_B$ ) (1). The local magnetic moments appear to be strongly reduced, however, on going to dimers and chains, as shown by neutron diffraction data ( $\mu = 2S \mu_B$ :  $1.9 \mu_B$ ,  $\text{KFeS}_2$ ;  $1.8 \mu_B$ ,  $\text{RbFeS}_2$  (5)) and magnetic hyperfine fields from Mössbauer experiments (221 kG for  $\text{KFeS}_2$  and 192 kG for  $\text{RbFeS}_2$  (6a, 6b)), which are small compared to the mostly ionic  $\text{Fe}^{3+}$  oxides and fluorides (350–550 kG). A spin-pairing mechanism ( $S = 1/2$ ) has been proposed, with the aim of explaining also the magnetic susceptibility data of  $\text{CsGa}_{1-x}\text{Fe}_x\text{S}_2$  ( $0 < x < 0.25$ ) in dependence on  $x$  (4). The Néel temperature of  $\text{KFeS}_2$  ( $T_N = 250$  K) reflects a three-dimensional magnetic ordering composed of a strong correlation between spins within the chain and a rather weak spin-coupling between

chains. However, cooperative effects (antiferromagnetic coupling) strongly complicate such an  $S = 1/2$  spin interpretation. Cooperative optical effects are also indicated by the polarized spectra on the  $\text{CsGa}_{1-x}\text{Fe}_x\text{S}_2$  mixed crystals, as manifested by the strong dichroism in the visible region and the near-band edge intensity shape in polarization parallel to the chain, even at  $\text{Fe}^{3+}$  concentrations as low as 1% (7). The absorption spectra of the pure chain compounds are dominated by three broad maxima at 15,100, 18,800, and 23,000  $\text{cm}^{-1}$  and have been ascribed to  $d-d$  transitions within the high-spin  $d^5 \text{FeS}_4^{2-}$  chromophore (8). A subsequent reinterpretation based on the high intensity, in terms of a ligand-to-metal charge transfer transition, has been proposed (7), while the weaker features between 8000 and 17,000  $\text{cm}^{-1}$  in the  $\text{Fe}^{III}$ -doped  $\text{CsGeS}_2$  have been attributed to purely  $d-d$  transitions within the  $d^5$  states manifold.

In the studies so far, interpretations of magnetic and optic data on these compounds have been confined to ligand-field calculations within the  $d^5$  configurations (7, 8, 15), or to extended Hückel or unrestricted Hartree-Fock calculations of the orbital levels (9, 10), disregarding the important role of correlation effects. Attempts to account for the latter have been made with variable success using the  $X_\alpha$ -SW MO method (11, 12, 13a, 13b) and in the broken symmetry spin-polarized  $X_\alpha$ -VB-SW calculations (12, 14). In ligand-field treatments, interactions of  $d^5$  with the  $d^6L$  ( $L$  hole on the ligand) charge transfer states are accounted for in an effective way by an appropriate choice of the one-electron parameters of the ligand field from a fit to the experimental data. Thus it is tacitly assumed that  $d^5$  and  $d^6L$  multiplets are energetically well separated, which certainly is not valid for the rather covalent Fe-S bond. Experimental data indicate, indeed, that the  $S^{2-}$  orbitals are rather close in energy to the  $3d$  orbitals. Attempts to explain the reduced magnetic moments within the same approach have been given in terms of an  $S = 1/2$  ground state of  $\text{Fe}^{3+}$  in the chains and even an intermediate  $S = 3/2$  local spin state for the dimers (16).

In this paper  $2p^63d^5 \rightarrow 2p^53d^6$  high-resolution X-ray absorption spectra on  $\text{KFeS}_2$  containing  $\text{FeS}_2$  chains are reported and compared with the spectra of  $\text{Na}_5\text{FeS}_4$  containing separate  $\text{FeS}_4^{2-}$  ( $S = 5/2$ ) units. We show that the local spin states in both compounds are the same ( $S = 5/2$ ), excluding the  $S = 1/2$  and  $S = 3/2$  states as possible alternatives. An interpretation of the spectral band shapes in terms of a model Hamiltonian which takes explicit account of the  $d^6L$  and  $d^7L^2$  charge transfer states provides an indication for the model parameters from a fit to the observed band profiles. The model parameters are compared with Harrison-like (17) calculations of the orbital levels for  $\text{Fe}^{3+}$ , which interact with the MO orbitals of representative  $\text{S}_4^{2-}$  and  $\text{S}_8^{6-}$  clusters. A discussion of the changes in the absorption profiles on going from  $\text{Na}_5\text{FeS}_4$

to  $\text{KFeS}_2$  will be given. Using calculations within the  $d^5$ – $d^6L$ – $d^7L^2$  configuration–interaction cluster model, a reinterpretation of the optical results is proposed as well. Finally, we will study in more detail the possible ground state spin multiplicities for  $d^5$  ions in a tetrahedral field and the dependence on the parameters of the cluster CI model. Parameter ranges for high ( $S = 5/2$ ), low ( $S = 1/2$ ), and even intermediate ( $S = 3/2$ ) spin states will be specified. In view of the possibility for ground states with a spin  $S = 3/2$  in cases of negative to small ligand-to-metal charge transfer energies, limits for the application of the well-known Tanabe–Sugano diagrams are discussed.

## II. EXPERIMENTAL

The X-ray absorption spectra (XAS) at the  $\text{Fe}2p$  edge were taken at the undulator 5U.1 at the SRS Daresbury. A number of crystals of both  $\text{Na}_5\text{FeS}_4$  and  $\text{KFeS}_2$  were measured in order to ensure consistency and reproducibility. All spectra were collected in a vacuum range of  $10^{-7}$ – $10^{-8}$  Torr. The spectra were taken in total electron yield mode, using a channeltron. The resolution at the  $\text{Fe}2p$  edge was about 450 meV.

In order to analyze the experimental data, a large number of multiplet energy and X-ray absorption intensity calculations were performed, using the chain groups approach given by Butler (18). This approach starts with the calculations of the reduced matrix elements of all necessary operators in the spherical group, realized using Cowan's atomic multiplet program (19a, 19b). The Wigner–Eckart theorem is then applied to obtain the reduced matrix elements in any desired point group. Butler's point-group program calculates the necessary isoscalar factors, using modern group theoretical results to obtain a consistent set of coefficients. Using this approach, a general program was developed by Thole (20a; see 20b–20d) with the advantage over standard methods of treating all point groups in a uniform way. The program can calculate transition energies and rates between any two configurations in X-ray absorption, photoemission, or inverse photoemission spectroscopy. The parameters used in these calculations, the  $d$ – $d$  Coulomb repulsion energy  $U$ , the core-hole– $d$ -electron Coulomb interaction  $Q$ , the ligand-to-metal charge transfer energy  $\Delta$ , the metal–ligand overlap energies  $T_c$  and  $T_t$ , and the crystal field  $10Dq$ , are treated as adjustable parameters. The  $d$ – $d$  Coulomb repulsion energy ( $U$ ) is defined by

$$U = E(d^6) + E(d^4) - 2E(d^5), \quad [1]$$

where  $E(3d^6)$ ,  $E(3d^4)$ , and  $E(3d^5)$  denote the configuration-averaged energies of the  $3d^6$ ,  $3d^4$ , and the  $3d^5$  multiplets, respectively. In addition, the charge transfer energy

$\Delta$  is by definition  $E(3d^{n+1}L) - E(3d^n)$ , where  $E(3d^{n+1}L)$  and  $E(3d^n)$  denote the configuration-averaged energies of the  $3d^{n+1}L$  and  $3d^n$  multiplets, respectively. The parameter  $\Delta_{\text{eff}}$  for  $\text{Fe}^{3+}$  ( $d^5$ ) is defined with respect to the respective ground states of the  $d^5$  and  $d^6L$  multiplets:

$$\Delta_{\text{eff}} = \Delta + (28/9)J, \quad [2]$$

The parameter  $U_{\text{eff}}$ , which for the  $\text{Fe}^{3+}$  ( $d^5$ ) is defined with respect to the respective  $3d^6$ ,  $3d^4$ , and  $3d^5$  ground states is related to  $U$  as

$$U_{\text{eff}} = U + (56/9)J, \quad [3]$$

where

$$J = 3B + C \quad [4]$$

is taken as the average from the intra-atomic (Hund) exchange integrals between  $e$  electrons ( $4B + C$ ),  $t_2$  electrons ( $3B + C$ ), and between  $e$  and  $t_2$  electrons ( $2B + C$ ). The values of the Racah parameters  $B$  and  $C$  (and the related  $F^2(d, d)$ ,  $F^4(d, d)$  parameters) were reduced to 80% of their atomic Hartree–Fock values to account for intra-atomic relaxation effects (19b). A list of ab initio Hartree–Fock values for the initial and final state configurations, including Fe  $2p$ – $3d$  Coulomb [ $F^2(p, d)$ ,  $G^1(p, d)$  and  $G^3(p, d)$ ] and spin–orbit coupling parameters  $\zeta(3d)$  and  $\zeta(2p)$ , is given in Table 1.

## III. RESULTS AND DISCUSSION

### III.1. $L_{2,3}$ –X-Ray Absorption Spectra and the Spin State of $\text{Fe}^{III}$ in $\text{Na}_5\text{FeS}_4$ and $\text{KFeS}_2$

The experimental  $2p \rightarrow 3d$  XAS spectra of  $\text{Na}_5\text{FeS}_4$  and  $\text{KFeS}_2$  are depicted in Fig. 2. They consist of  $2p_{3/2}(L_3)$  and  $2p_{1/2}(L_2)$  branches with an energy separation of  $1.5\zeta_p$ , where  $\zeta_p$  is the spin–orbit coupling constant. Comparing the spectra of  $\text{Na}_5\text{FeS}_4$  with isolated  $\text{FeS}_4^{5-}$  units ( $S = 5/2$  ground state) with the spectrum of  $\text{KFeS}_2$  with interconnected  $\text{FeS}_4^{5-}$  polyhedra, one can state that (aside from some changes which will be discussed subsequently) the spectra are very similar. Comparing the details of the multiplet structure of experimental X-ray absorption spectra with atomic multiplet calculations provides a powerful tool for determining the local spin state of  $3d$  transition metal ions in their compounds. The multiplet structure arises from the transitions  $2p^63d^n \rightarrow 2p^53d^{n+1}$ , where dipole selection rules strongly confine the subset of final states that can be reached from the ground state. In the low-spin ground state, electrons pair up in orbitals with the lowest energy, while in the high-spin ground state higher orbitals are also occupied with the spins parallel. In the five-particle

TABLE 1  
Ab initio Hartree-Fock Values of the Parameters (eV) of the Initial and Final State Configurations

	$F^2(d,d)$ (B)	$F^4(d,d)$ (C)	$J$	$\zeta(3d)$	$F^2(p,d)$	$G^1(p,d)$	$G^3(p,d)$	$\zeta(2p)$
$Fe^{3+}2p^63d^5$	12.043 (0.160)	7.535 (0.598)	1.079	0.059	—	—	—	—
$Fe^{2+}2p^63d^6$	10.966 (0.146)	6.815 (0.541)	0.980	0.052	—	—	—	—
$Fe^{1+}2p^63d^7$	9.762 (0.131)	6.018 (0.478)	0.870	0.046	—	—	—	—
$Fe^{3+}2p^53d^6$	12.818 (0.171)	8.023 (0.637)	1.149	0.074	7.446	5.566	3.166	8.199
$Fe^{2+}2p^53d^7$	11.779 (0.157)	7.327 (0.582)	1.053	0.067	6.793	5.004	2.844	8.200
$Fe^{1+}2p^53d^8$	10.623 (0.142)	6.560 (0.521)	0.948	0.059	6.143	4.467	2.538	8.202

Note. The actual values for the Coulomb and exchange interactions have been scaled to 80% of these values. Spin-orbit coupling parameters  $\zeta(3d)$  and  $\zeta(2p)$  are taken without reduction.

case of  $Fe^{3+}(d^5)$  this results in distinctly different types of XAS spectra, which can be used as a fingerprint for high spin or low spin. Crystal-field interaction mixes states with different  $L$  in the ground  $LS$ -term, allowing transitions to other final states with the same spin. This gives rise to a broadening of the peaks and a gradual appearance of new peaks with increasing crystal field strength (10Dq). XAS profiles for  $Fe(d^5)$  in  $T_d$  coordination and variable cubic splitting, 10Dq values are depicted in Fig. 3 (adopted from Ref. (20c)). In these calculations hybridization<sup>2</sup> was not taken into account. With increasing 10Dq a change from  $S = 5/2$  to  $S = 1/2$  takes place when the 10Dq parameter becomes larger than the  $5/2 \rightarrow 1/2$  spin-pairing energy. In the same direction the weaker transition at the higher energy side of the  $L_3$  branch disappears, while an additional transition at the lower energy side of the  $L_3$  branch grows in intensity. Comparison of Fig. 3 with the experimental spectrum in Fig. 2 lends further support to the idea that both compounds  $Na_5FeS_4$  and  $KFeS_2$  are characterized by similar parameter values appropriate for a high-spin  $S = 5/2$  ground state.

### III.2. XAS and Covalency Effects in $FeS_4$ Clusters: A Charge Transfer Model for the Fe-S Bonding

III.2.1. The spectrum of  $Na_5FeS_4$ . In the previous section only crystal-field effects have been taken into account. The cubic symmetry is accounted for in terms of a single parameter, 10Dq, the role of which is just to split the  $d$  orbitals in cubic symmetry into two-  $e(x^2-y^2, 3z^2-r^2)$  and threefold  $t_2(xy, xz, \text{ and } yz)$  degenerate sublevels. In the

following, covalency effects due to hybridization of the  $d^5$  with the  $d^6L$  and  $d^7L$  charge transfer states, which were neglected in previous studies, will be explicitly considered. A schematic presentation of the coupling of electronic configurations in the initial and final states with appropriate parameters is illustrated in Fig. 4.

Diagonal matrix elements are parametrized in terms of the parameters of  $3d-3d$  and  $2p-3d$  Coulomb interactions  $U$  and  $Q$ , respectively (see Section II).

The initial and final states originating from the ionic  $Fe^{3+} 2p^63d^5$  and  $2p^53d^6$  states couple with the multiplets of the same symmetry which result from transferring a single electron from the  $3p$  orbitals of S to Fe ( $2p^63d^6L$  and  $2p^5d^7L$ , respectively). The nearest neighbor ligand-to-metal  $2p-3d$  hopping elements, which couple the ionic

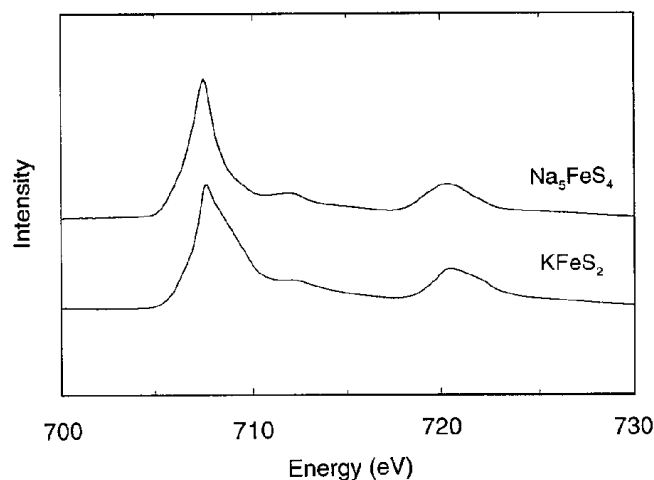


FIG. 2. Experimental  $Fe2p$  XAS data on  $Na_5FeS_4$  (isolated  $FeS_4$  tetrahedra) and  $KFeS_2$  (edge-sharing  $FeS_4$  tetrahedra).

<sup>2</sup> Hybridization, used in a different sense than in chemistry, means the interaction of orbitals of different centers via the effective one-electron Hamiltonian.

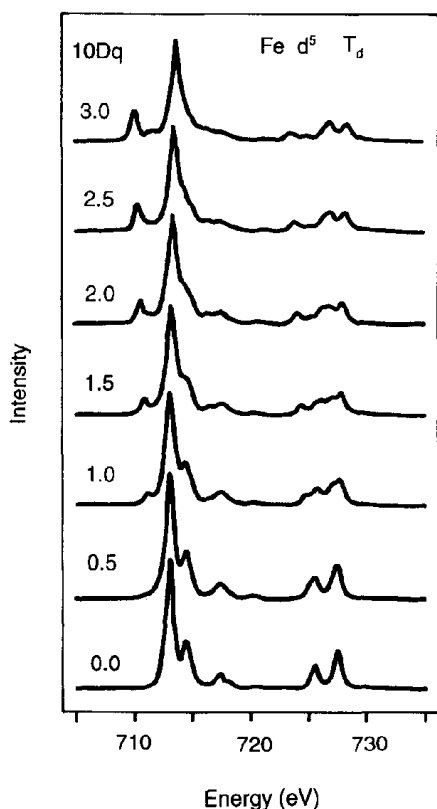


FIG. 3. Calculated  $2p$  absorption spectra for  $\text{Fe}^{3+}(d^5)$  in tetrahedral ( $T_d$ ) geometry (adopted from Ref. (20c)). The Slater integrals and spin-orbit parameters are 80 and 100% of the free ionic values, respectively.

$d^5$  states with the  $d^6L$  and the  $d^6L$  with the  $d^7L^2$  charge transfer states, are expressed in terms of Slater-Coster integrals ( $pd\sigma$ ) and ( $pd\pi$ ) (21).  $T_i$  and  $T_e$  integrals are introduced to represent hybridization between the  $3d$  orbitals of  $t_2$  and  $e$  symmetry, respectively, and the corresponding ligand orbitals of the same symmetry.

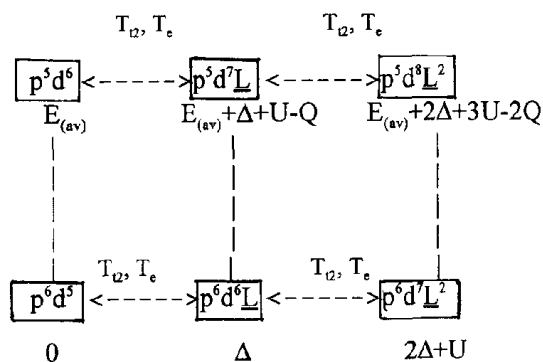


FIG. 4. A parametric scheme for the XAS initial and final states and their energies for  $d^5$  ions including hybridization with singly and doubly excited ligand-to-metal charge transfer configurations. For a definition of the model parameters, see text.

The contributions to  $T_i$  and  $T_e$  are easily calculated using the one-electron secular matrices:

$$\begin{pmatrix} t_2[d^5] & t_2[d^6L(\sigma)] & t_2[d^6L(\pi)] \\ 0 & [(2/\sqrt{3})(pd\sigma)] & [(2\sqrt{2}/3)(pd\pi)] \\ [(2/\sqrt{3})(pd\sigma)] & \delta & 0 \\ [(2\sqrt{2}/3)(pd\pi)] & 0 & \delta \end{pmatrix} \quad [5]$$

$$\begin{pmatrix} e(d^5) & e[d^6L(\pi)] \\ 0 & [2\sqrt{(2/3)}(pd\pi)] \\ [2\sqrt{(2/3)}(pd\pi)] & \delta \end{pmatrix} \quad [6]$$

In these equations we used  $\delta$  as a notation of the orbital transfer energy as defined by the energy separation between the baricenters of the  $e$ ,  $t_2$  orbitals of the metal and the ligands. The following relationship between the parameters  $\delta$  and  $\Delta_{\text{eff}}$  can be derived if one takes the  ${}^6A_1(d^5)$  and  ${}^6A_1[d^6t_2(L)]$  terms as energy references for  $d^5$  and  $d^6L$ , respectively:

$$\Delta_{\text{eff}} = \delta + 4Dq + 5U. \quad [7]$$

Note that the coupling between the  $e$  orbitals is represented by a single parameter  $T_e = [2\sqrt{(2/3)}(pd\pi)]$  (Eq. [6]), reflecting the covalent mixing between the  $d^5$  and the  $d^6L$  multiplets, for orbitals of  $e$  type, while two independent parameters,  $T_i(\sigma) = [(2/\sqrt{3})(pd\sigma)]$  and  $T_i(\pi) = [(2\sqrt{2}/3)(pd\pi)]$ , are needed for orbitals of  $t_2$  type (Eq. [5]). This results in a markedly different bonding scheme as compared to octahedral complexes, where ligand orbitals contribute by unique combinations of  $e_g(\sigma)$  and  $t_{2g}(\pi)$  symmetries.

In Eqs. [5] and [6] ligand-ligand hybridization is not taken into account. In order to study the effect of the latter as well as to obtain greater insight into the effects of covalency influencing the parameter values  $T_e$  and  $T_i$ , we performed calculations on the  $\text{FeS}_4^{3-}$  clusters, using the method of Harrison (17) to estimate the matrix elements of metal-ligand,  $V_{ldm}$ , and ligand-ligand,  $V_{llm}$  ( $m = \sigma, \pi$ ), covalent mixing. The problem is divided into two steps. In the first step the orbitals  $\Psi_l^+$  and energies  $E_l^+$  of a  $S_4^{3-}$  tetrahedral cluster are obtained, considering ligand-ligand orbital coupling matrix elements only. In a second step, the coupling of the  $3d$  orbitals with the resulting  $S_4^{3-}$  cluster orbitals  $\Psi_l^+$  are evaluated, yielding matrix elements for the  $t_2$  and  $e$  symmetry species. The energies of the  $\text{Fe}^{3+}$ ,  $3d$  and  $S^{2-}$ ,  $3p$ ,  $3s$  orbitals have been taken as  $-12.70$ ,  $-13.30$ , and  $-20.00$  eV, respectively (9). The resulting secular equations for the  $e$ - and  $t_2$  symmetries are listed in Table

TABLE 2

$S_4^{3-}$  Cluster Orbital Energies and Matrix Elements (in eV) of  $[Fe^{3+}, 3d]-[S_4^{3-}(3s,3p-MO)]$  Hybridization as Obtained from Harrison-type MO-LCAO Calculations<sup>a</sup>

$Fe^{3+}3d$ symmetry ( $T_d$ )	Cluster MO $i =$	1	2	3
$e$	$E_i$	-13.569		
	$(x^2 - y^2 H \Psi_i)$	0.728		
	$(3z^2 - r^2 H \Psi_i)$			
$t_2$	$E_i$	-13.797	-12.256	-19.526
	$(xy H \Psi_i)$			
	$(xz H \Psi_i)$	-0.121	1.410	-0.774
	$(yz H \Psi_i)$			

<sup>a</sup> Orbital energies adopted from Ref. (9) are  $E(3p, S^{2-}) = -20.00$  eV,  $E(3s, S^{2-}) = -13.3$  eV  $E(3d, Fe^{3+}) = -12.7$  eV.

2. The  $t_2$  coupling matrix can be reduced in a rather good approximation to a  $(2 \times 2)$  problem, involving the  $3d$  and  $\Psi_2(L, 3p)$  basis functions only. The contributions from the functions  $\Psi_1(L, 3p)$  and  $\Psi_3(L, 3s)$  can be neglected; the first is essentially nonbonding, as is seen by the small  $3d-3p$  off-diagonal element, the second ( $3s$  type) is fairly well separated in energy from  $3d$ , yielding negligible coupling. It follows from these considerations that the basis set of the  $t_2$  orbitals can be reduced in a rather good approximation to two basis functions of ligand and metal type, which mix by covalency via a single (effective) quantity denoted hereafter by  $T_t$ . The calculated value of  $T_t$  (1.410 eV) is found to be twice as large as the hopping integral of  $e$  type ( $T_e = 0.728$  eV) (compare to the octahedral case where a  $T_e/T_t$  ratio of 2 has been proposed (22)). The splitting of the ligand orbitals  $t_2$  and  $e$  we define as  $\delta W = E[t_2(L)] - E[e(L)]$  is calculated to be 1.3 eV.<sup>3</sup>

The results from the cluster calculations have been used to reduce the number of model parameters as follows: the splitting of the ligand levels  $\delta W$  and the  $T_e/T_t$  parameter ratio were fixed at 1.3 eV and 0.5, respectively. Values of  $U$  and  $Q$  of 6 and 5 eV were adopted from data on related systems and a  $Q/U$  value of 0.83 (23a, 23b). The parameters  $T_t$ ,  $\Delta$ , and  $10Dq$  were treated as adjustable parameters. The experimental spectrum together with the calculated spectra for high-, intermediate-, and low-spin ground states are shown in Fig. 5, while the parameters used in these calculations are listed in Table 3.

The calculated band shape was found to be most sensitive with respect to  $10Dq$  and  $T_t$  and to a lesser extent to the parameters  $\Delta$ ,  $U$ ,  $Q$ , and  $\delta W$ . The feature at the high-energy side seen in the experimental  $L_3$  edge of  $Na_5FeS_4$  (Fig. 2) could be only reproduced for values of  $10Dq$  with

<sup>3</sup> With nonzero values of  $\delta W$  Eq. [7] must be modified as  $\Delta_{\text{eff}} = \delta + 4Dq - (2/5)\delta W + 5U$ .

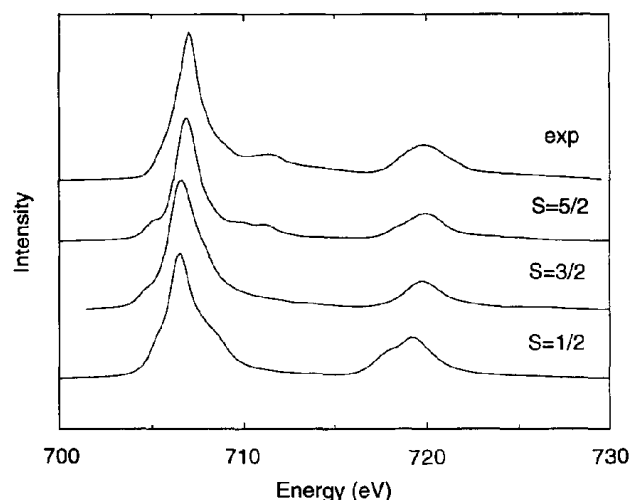


FIG. 5. Experimental and theoretical XAS spectra for  $Na_5FeS_4$ . Calculations for the high- ( $S = 5/2$ ), intermediate- ( $S = 3/2$ ), and low-spin ( $S = 1/2$ ) initial states have been done with parameter values, listed in Table 2.

a high-spin ground state on  $Fe^{3+}$ . The negative value of  $\Delta$  shows that the center of gravity of the  $d^6L$  charge transfer states is at lower energy than the  $d^5$  states (but note the still positive value for  $\Delta_{\text{eff}}$  (Eq. [2],  $\Delta_{\text{eff}} = 0.68$  eV). However, there is a strong mixing between the two configurations as well as a small yet nonnegligible  $d^7L^2$  contribution in the ground state:

$$\Psi_{\text{g.st.}} = \sqrt{(0.41)}|d^5\rangle + \sqrt{(0.52)}|d^6L\rangle + \sqrt{(0.07)}|d^7L^2\rangle. \quad [8]$$

The parameters  $\Delta$  and  $T_t$  (Table 3) are comparable in sign and magnitude to those obtained from a recent study of the valence band photoemission spectra of the chalcopyrite-type  $CuFeS_2$  compound ( $\Delta = -0.5$  eV,  $U = 4$  eV) (24) but are markedly different compared to the parameter range for  $\Delta$  (1.9–5.0 eV), deduced from core-level XPS spectra of  $KFeS_2$  reported by Butcher *et al.* (25). One possible reason for this disagreement is the covalent mixing

TABLE 3

Summary of the Parameters (in eV) Used in the Calculation of the  $L_{2,3}$ -Edge XAS of  $Na_5FeS_4$  for High- ( $S = 5/2$ ), Intermediate- ( $S = 3/2$ ), and Low-Spin ( $S = 1/2$ ) Initial States

$S$	$\Delta$	$T_t$	$T_e$	$10Dq$
5/2	-2.0	1.4	0.7	0.5
3/2	-5.0	1.4	0.7	0.78
1/2	-2.0	1.4	0.7	2.0

Note. In all three calculations  $U$ ,  $Q$ , and  $\delta W$  have been taken to be 5.0, 6.0, and 1.3 eV, respectively (see text).

matrix element  $T = \langle d|H|L \rangle$ , which was approximated in (25) as being the same for the  $e$  and the  $t_2$  orbitals.

**III.2.2. The spectrum of  $KFeS_2$ .** As seen from Fig. 2, the  $L_{2,3}$  edges of  $Na_5FeS_4$  and  $KFeS_2$  show a striking similarity with respect to their band shapes and maxima positions. However, there is a clear broadening of the main peak toward the high-energy side when going from  $Na_5FeS_4$  to  $KFeS_2$  (Fig. 2). Using the configuration interaction–charge transfer model described in Section III.2.1, we tried to reproduce the band shape by varying the model parameters  $10Dq$ ,  $T_t$ , and  $\Delta$ . We were not able to reproduce the intensity distribution while maintaining the spectral features of the experimental spectrum. Starting with the parameters used in the  $Na_5FeS_4$  calculation (Table 3, high-spin values), small changes in  $10Dq$ ,  $\Delta$ , and  $T_t$  have little effect on the width of the main peak. Large variations alter the spectrum to a large extent when the spin of the ground state is changed. In particular, the shoulder at the high-energy side of the  $L_3$  edge is not compatible with  $S = 1/2$  and  $S = 3/2$  ground states. In view of this, it is still the high-spin state which reproduces the overall spectral features of  $KFeS_2$ . However, the broadening indicates that upon going from separate to interconnected  $FeS_4^{5-}$  tetrahedra, the electronic levels of the high-spin  $Fe^{3+}$  are modified considerably by the presence of neighboring  $FeS_4^{5-}$  centers. Although superexchange has been recently shown to influence the XAS spectral shapes (26, 27a, 27b), the size of the effect is too small to explain the observed broadening.

Another contribution affecting the multiplet energies of  $Fe^{3+}$  originates from low symmetric fields due to ligand–ligand interactions as well as the perturbing effect of neighboring  $Fe^{3+}$  ions. The latter influences are electrostatic in origin and were explicitly accounted for by Bronger and Müller (15), who calculated the crystal field effect on a given  $Fe^{3+}$  induced by the  $S^{2-}$  in  $Fe^{3+}$  in the particular lattice sites. However, as follows from our consideration, the electrostatic charges of  $Fe^{3+}$  and  $S^{2-}$  should be strongly reduced by the rather covalent Fe–S interactions, leading to a rather small effect of  $Fe^{3+}$  on neighboring  $Fe^{3+}$  centers. In support of this, spin-polarized Slater  $X\alpha$  calculations give net charges on  $Fe^{3+}$  (+1.2) distinctly smaller than those assumed in the electrostatic calculation (15).

The second aspect concerns the bonding properties of  $S^{2-}$ , which may considerably change going from separate to interconnected  $FeS_4^{5-}$  units. As was shown by Silvestre and Hoffman (9), the orbitals of  $S^{2-}$  in the separate  $FeS_4^{5-}$  tetrahedra are optimally aligned for interactions between  $Fe^{3+}$  and  $S^{2-}$ . In a chain composed of  $FeS_4^{5-}$  tetrahedra connected via common edges, the orbitals of  $S^{2-}$  are shared between two tetrahedra and as such cannot be optimally aligned with respect to the metal–ligand and the ligand–ligand interactions at the same time. Thus, orbitals which contribute to  $\sigma$  bonding with iron ( $t_2$ ) will be involved in weaker  $\pi$  interactions with neighboring sulfur atoms so

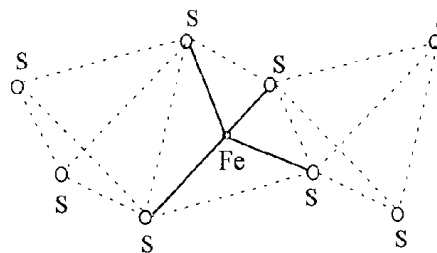


FIG. 6. The  $S_8^{16-}$  cluster hybridizing the  $3d$  orbitals of  $Fe^{3+}$  placed at the position of the central  $S_4^8$  tetrahedron. The site symmetry around  $Fe^{3+}$  is  $D_{2d}$ , the geometry of the nearest  $S_4^8$  surrounding of  $Fe^{3+}$ , is regular tetrahedral.

that they will be insensitive with respect to increasing the cluster size. In contrast, going to the chain the only weakly  $\pi$ -interacting  $e$  orbitals of S acquire some  $\sigma$ -bonding components as well, inducing a stronger energy effect on the corresponding orbitals on the metal. The result of all these influences is a low symmetric field seen by each  $Fe^{3+}$  center even though the  $S^{2-}$  ions taken as point charges form regular tetrahedra around  $Fe^{3+}$ .

We modeled the effect of ligand–ligand coupling by calculating the orbital levels of a  $S_8^{16-}$  cluster consisting of three  $S_4^8$  moieties with a regular tetrahedral geometry (Fig. 6). Orbital matrix elements between ligands  $3p$  and  $3s$  basis functions were approximated, using formulas by Harrison (17) (see above). The resulting eigenfunctions were coupled with the  $3d$  orbitals of  $Fe^{3+}$  placed at the central tetrahedral unit. The matrix elements between the various  $3d$  orbitals of iron and their counterparts of appropriate symmetry from the  $S_8^{16-}$  cluster orbital levels are included in Table 4. The resulting secular equations, each including a single  $d$  orbital were diagonalized. The energy levels for the eigenfunctions of the  $FeS_8^{13-}$  with main participation from the  $3d$  orbitals of Fe are depicted in Fig. 7 (dashed lines) and can be compared with the corresponding orbitals of a single  $FeS_4^{5-}$  moiety (solid lines).  $d$  Orbital percentages are also indicated.

There is a considerable splitting of the  $3d$  orbitals of  $Fe^{3+}$ , reflecting the symmetry lowering from  $T_d$  to  $D_{2d}$  around iron in the  $FeS_8^{13-}$  cluster, compared with the separate  $FeS_4^{5-}$  units. Note that the  $S_4^8$  point geometries in both calculations were taken as regular tetrahedra. As seen in Fig. 7, the energy changes are particularly pronounced for the  $z^2$ -type orbital, which also undergoes the most reduction in its  $3d$  character (about twice that in  $FeS_4^{5-}$ ). The reduction in the  $d$ -orbital percentage follows the energy shifts, as expected. The incorporation of the  $Fe^{3+}$  ions into the extended  $S_8^{16-}$  compared to the smaller  $S_4^8$  cluster also leads to a shift in  $z^2$  to an approximately 0.5-eV higher energy. The lowering of symmetry could explain the broadening of the  $2p \rightarrow 3d$  absorption profile toward the high-energy side going from  $Na_5FeS_4$  to  $KFeS_2$ . Also in strong

TABLE 4  
 $S_8^{16-}$  Cluster Orbital Energies and Matrix Elements (in eV) of  $[Fe^{3+}, 3d]-[S_4^{8-} (3s, 3p-MO)]$  Hybridization as Obtained from Harrison-type MO-LCAO Calculations<sup>a</sup>

Fe <sup>3+</sup> 3d cluster MO (symmetry $D_{2d}$ )	$i =$	1	2	3	4	5	6	7	8
$b_1$	$E_i$	-13.792	-12.919						
	$(x^2 - y^2 H \Psi_i)$	0.609	0.400						
$a_1$	$E_i$	-21.910	-19.973	-14.261	-14.073	-13.675	-12.214		
	$(3z^2 - r^2 H \Psi_i)$	0.019	-0.066	-0.308	-0.336	0.191	-0.543		
$b_2$	$E_i$	-21.125	-18.836	-14.155	-13.730	-12.626	-12.063		
	$(xy H \Psi_i)$	-0.373	0.681	0.029	-0.109	-0.866	1.112		
$e$	$E_i$	-19.596	-19.486	-14.090	-13.575	-12.942	-12.513	-12.275	-12.001
	$(xy, yz H \Psi_i)$	-0.600	0.484	-0.066	0.090	0.473	-0.463	-0.678	1.050

<sup>a</sup> Orbital energies adopted from ref. (9) are  $E(3p, S^{2-}) = -20.0$  eV;  $E(3s, S^{2-}) = -13.3$  eV;  $E(3d, Fe^{3+}) = -12.7$  eV.

support of the low-symmetric field around  $Fe^{3+}$  in the extended  $S_8^{16-}$  tetrahedral arrays is the polarization seen in the optical spectra (7) and the electric field gradients from Mössbauer data (6). The quadrupolar splittings manifested by the Mössbauer experiments range between 0.51 (KFeS<sub>2</sub>) and 0.44 mm · s<sup>-1</sup> (CsFeS<sub>2</sub>) and can be attributed to overlap distortions of the 3p levels of Fe imposed by the surrounding ligands (28). As follows from the expres-

sions of the z components of the electric field gradient ( $q'_{ov}$ ) due to overlap contributions (28)

$$q'_{ov} = (4/5)e(r^{-3})_{3p}[2N_z^2 - N_x^2 - N_y^2]; \quad [8]$$

the orbital contributions from 3p<sub>z</sub>, ( $N_z$ ) and 3p<sub>x</sub>, 3p<sub>y</sub> ( $N_x$ ,  $N_y$ ) become essentially different in the lowered ( $D_{2d}$ ) sym-

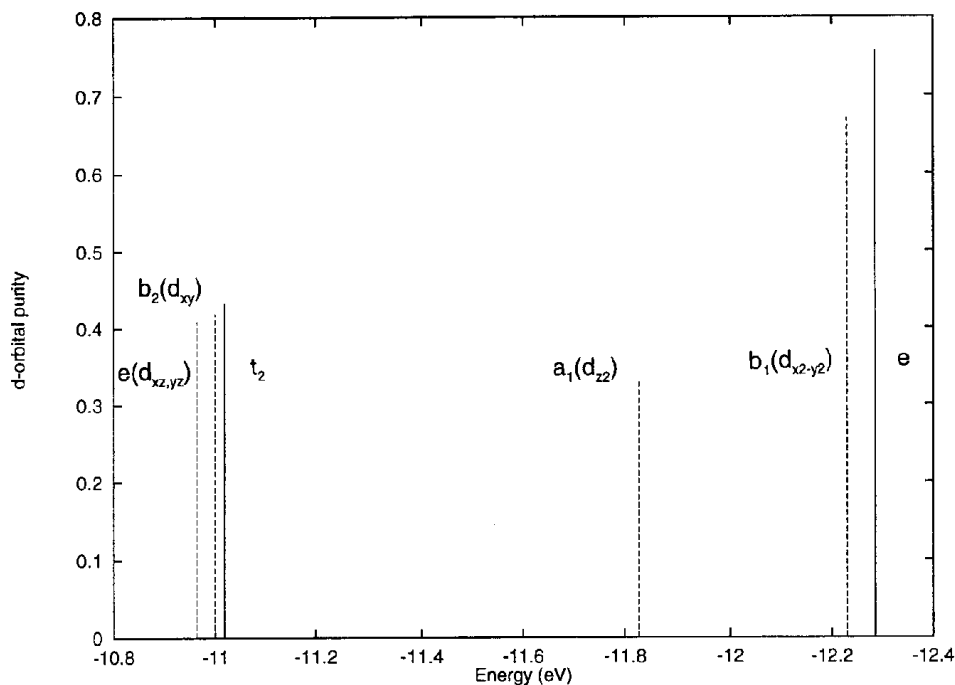


FIG. 7.  $d$  Orbital level scheme for an isolated  $FeS_4^{2-}$  tetrahedron ( $T_d$  symmetry, solid lines) and  $Fe^{3+}$  in  $S_8^{16-}$  (Fig. 6,  $D_{2d}$  symmetry, dashed lines). Orbital energies have been calculated using metal-ligand and ligand-ligand orbital matrix elements given by Harrison (Ref. (17)). Diagonal energies for the  $Fe^{3+}$  3d and  $S^{2-}$  3s, 3p orbitals have been adopted from Ref. (9). Note the splitting of the 3d orbitals of  $Fe^{3+}$  in the regular  $FeS_4$  units due to the lowered symmetry due to ligand-ligand coupling.



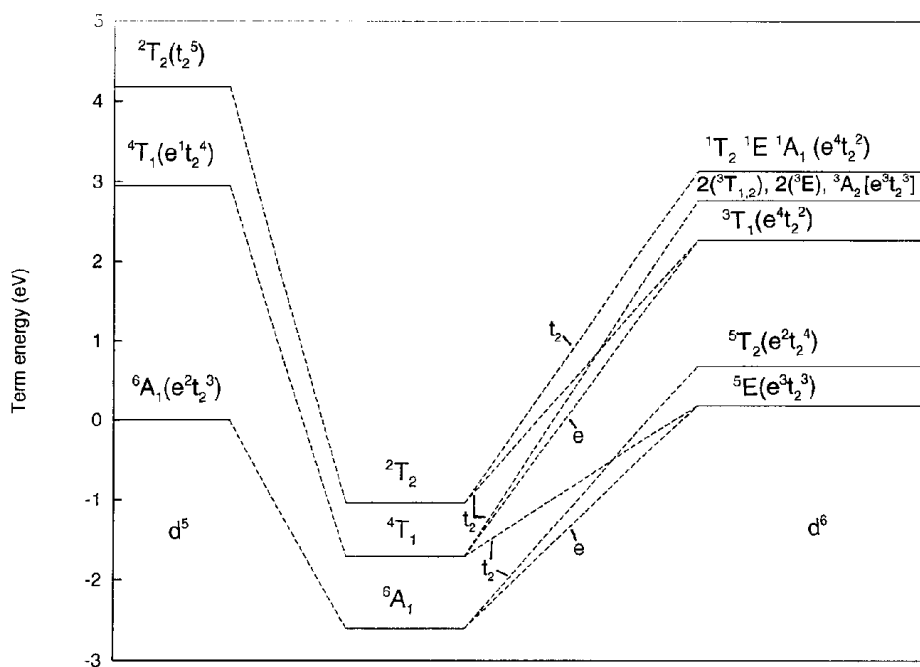


FIG. 8. The lowest ionic multiplets for  $d^5$  (left) and  $d^6L$  (right) and the resulting term energy diagram after accounting for their hybridization (middle). The  $d^7L^2$  states are not shown but have been taken into account in the calculations. For model parameters see Table 3 (high-spin ground state).

metry around  $\text{Fe}^{3+}$  in  $\text{KFeS}_2$ . No such contributions are expected for the only slightly distorted  $\text{FeS}_4$  tetrahedra in  $\text{Na}_5\text{FeS}_4$ . Unfortunately, Mössbauer data on this compound are lacking.

#### III.4. *d* Electronic Levels and the Spin-Forbidden Transitions in $\text{FeS}_4^{5-}$

Term energies have been calculated for the  $d^5$  configuration using parameters for the best fit [Table 2, high-spin ( $S = 5/2$ ) values]. Mixing with the  $d^6L$  and  $d^7L^2$  charge transfer states has been explicitly taken into account. A schematic term energy diagram, including the ground and the lowest excited states of  $d^5$  and  $d^6L$  before and after accounting for their hybridization, is presented in Fig. 8. States due to  $d^7L^2$  electronic configuration are not shown but have been taken into account in the numerical calculations. A list of theoretical values for the lowest transition energies as well the  $d^5$  percentages for the ground  ${}^6A_1$  and the first excited states  ${}^4T_1$ ,  ${}^4T_2$ , and  ${}^2T_2$  is given in Table 5. The calculated  ${}^6A_1 \rightarrow {}^4T_1$ ,  ${}^4T_2$ , and  ${}^2T_2$  transition energies (7180, 8630, and 12558  $\text{cm}^{-1}$ ) are in reasonable agreement with the experimental data reported by Solomon *et al.* for  $\text{Fe}(\text{SR})_4^-$  ( $R = 2,3,5,6\text{-Mc}_4\text{C}_6\text{H}$ , 7250, 7975, 9540, 10525, and 11235  $\text{cm}^{-1}$ ) (29), which show in addition low symmetric splitting of the tetrahedral parent  ${}^4T_1$  and  ${}^4T_2$  terms. Low-temperature absorption spectra in the near-IR and visible region on  $\text{Na}_5\text{FeS}_4$  and  $\text{CsGa}_{1-x}\text{Fe}_x\text{S}_2$  ( $0.0 < x < 0.25$ ) have been reported as well (7). However, the spectra

on the former compound were not very informative with regard to the spin-forbidden bands which overlap the more intense ligand-to-metal [ $t_1(L) \rightarrow 3d$ ] charge transfer transitions. The spectra of the latter compound were found to be affected by the lower symmetry already at low  $\text{Fe}^{3+}$  concentrations ( $x = 0.01$  (7)); aside from the fine structure due to this symmetry lowering, the experimental data are in support of the theoretical values in Table 5. It is seen from Fig. 8 and Table 5 that the  ${}^6A_1$  ground state is shared almost equally between the  $d^5$  and the  $d^6L$  configurations, while  $d^6L$  is the dominant contribution in the  ${}^4T_1$ ,  ${}^4T_2$ , and  ${}^2T_2$  excited states connected with the negative sign of the parameter  $\Delta$ , which places  $d^6L$  at a lower energy than  $d^5$ . The larger contribution of  $d^5$  to the ground state as compared to the lowest excited states is due to the gain of exchange energy, which is larger for the high-spin  $d^5$  compared to the doublet and quartet states. As follows

TABLE 5  
Transition Energies ( $\text{cm}^{-1}$ ) and  $d^5$  Percentage for the Ground and Lowest Excited States, Calculated Using a CI Charge Transfer Model for Tetrahedral  $\text{FeS}_4^{5-}$ <sup>a</sup>

State	${}^6A_1$	${}^4T_1$	${}^4T_2$	${}^2T_2$
Energy	0	7180	8630	12,560
% $d^5$	40	14	10	14

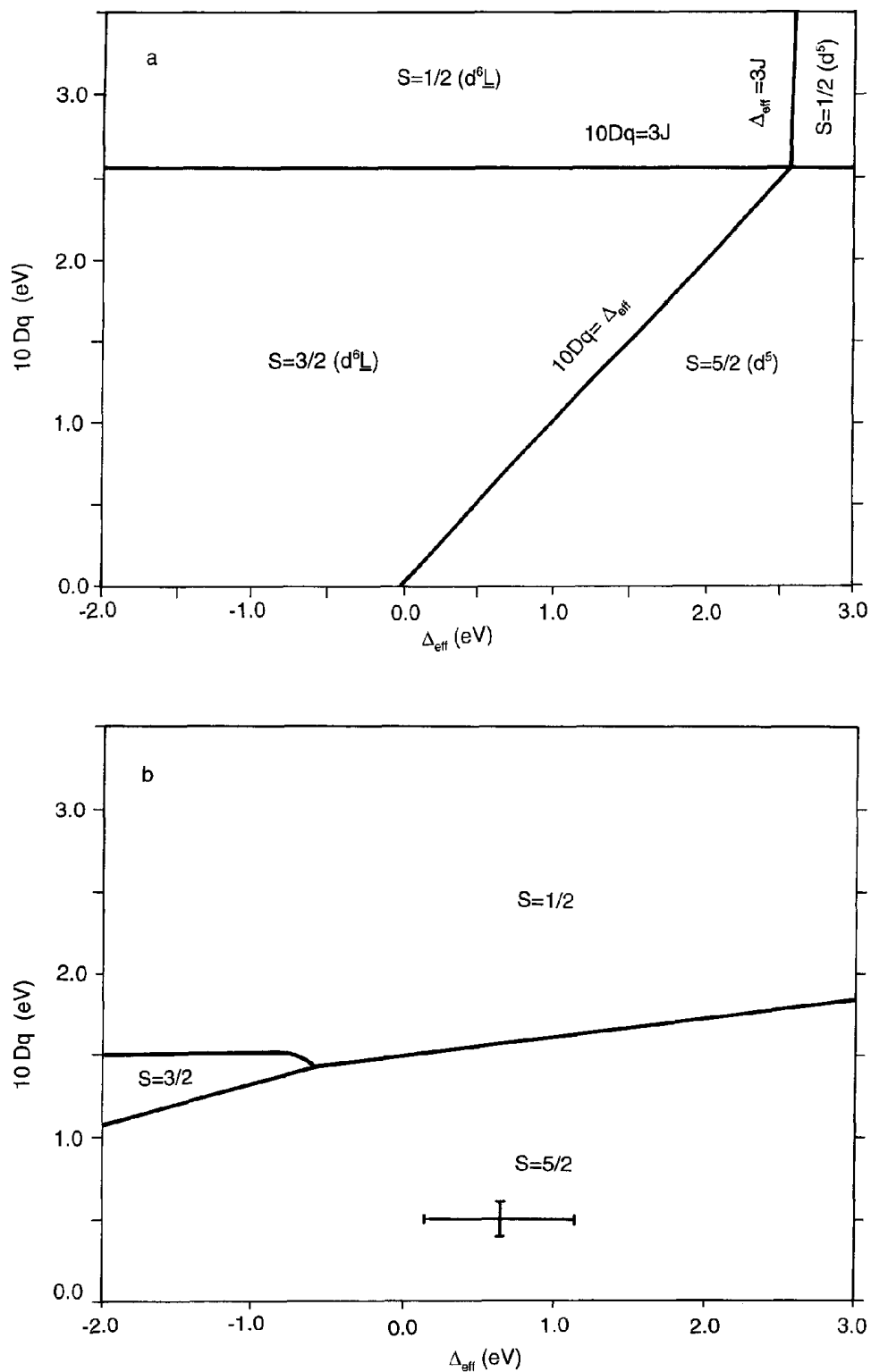
<sup>a</sup> Parameter values are  $\Delta = -2.0$  eV,  $10Dq = 0.5$  eV,  $T_1 = 1.4$  eV,  $T_2 = 0.7$  eV,  $U = 5$  eV, and  $Q = 6$  eV.

from Table 5 the transitions  ${}^6A_1 \rightarrow {}^4T_1$ ,  ${}^4T_2$ , and  ${}^2T_2$ , which are normally viewed as “ $d-d$ ” in a ligand field description, are in fact accompanied by a transfer of about 0.3 electrons from the metal to the ligand. This interpretation differs from the one proposed on the basis of spin-polarized  $X\alpha$  calculations, attributing these transitions to a partial transfer of one electron in the opposite direction (25). In both interpretations, however, a single electron is strongly delocalized on the ligands and the orbital composition changes on excitation. The difference in the two interpretations may result from the distinctly smaller (compared to Ref. (25)) value of the parameter  $\Delta$  indicated by our data. It was recently suggested (22) that ligand-field parametrization schemes such as the crystal field and the angular overlap models fail when the  $d^n$  and the  $d^{n+1}L$  charge transfer configurations become strongly intermixed. In this regime, multiplets due to  $d^5$  and  $d^6L$  couple to a different extent depending on their energy separation and hybridization. This prevents the use of a unique set of orbital and electron repulsion parameters as is usually done in ligand-field theory. Alternatively, any fitting procedure using such approaches may result in rather unrealistic parameter values [e.g., low values of  $B$  for  $\text{FeS}_4^{5-}$ ,  $B = 22 \text{ cm}^{-1}$ ; see (25),  $B(\text{free Fe}^{3+}) = 1100 \text{ cm}^{-1}$ ]. For such systems all symmetry aspects are still at work, as nicely reflected by Fig. 8; however, the ligand-field approach per se loses its quantitative power. A similar effect was also shown in the spin-forbidden transitions of high-valent tetraoxo-coordinate tetrahedral  $\text{Mn}^{5+}$  and  $\text{Fe}^{6+}$  ions (30).

### III.5. On the Spin-Ground States of $d^5$ Ions in Tetrahedral Coordination

The X-ray absorption data unambiguously show that the  $\text{FeS}_4^{5-}$  tetrahedra in both compounds  $\text{Na}_5\text{FeS}_4$  and  $\text{KFeS}_2$  are in a high-spin ground state. The intra-atomic exchange stabilization which favors the  $S = 5/2$  state apparently dominates the ligand-field stabilization, which tends to lower the  $S = 1/2$  and  $S = 3/2$  states energetically. According to the Tanabe–Sugano diagrams for  $d^5$  metals in cubic fields (31), intermediate spin states ( $S = 3/2$ ) cannot become the lowest in energy. However, the situation may drastically change when negative  $\Delta_{\text{eff}}$  values are allowed. In this case  $d^6L$  becomes lower in energy than  $d^5$  and the  $S = 3/2$  state may serve as alternative ground state of the  $\text{FeS}_4^{5-}$  cluster, ensuring high-spin local momenta ( $S = 2$ ) for  $\text{Fe}^{2+}(d^6)$ , in accordance with the Hund’s rule. An  $S = 3/2$  ground state has been suggested from the interpretation of the  $\text{Co}2p$  XAS spectrum for the  $d^5$  compound  $\text{SrCoO}_3$  (32). In view of these results, it would be interesting to see how variations in  $10Dq$  and  $\Delta_{\text{eff}}$  affect the spin state of lowest energy for the  $\text{FeS}_4^{5-}$  cluster. For this purpose we performed calculations restricting to the lowest energy states of high-, intermediate-, and low-spin,  $S = 5/2, 3/2,$

and  $1/2$ , respectively, for  $d^5$  and the corresponding  $d^6L$  and  $d^7L^2$  charge transfer states. A phase diagram indicating ranges of stability for the pure unmixed ground states ( $T_i = T_e = 0$ ) as a function of the parameters  $10Dq$  and  $\Delta_{\text{eff}}$  is plotted in Fig. 9a. The chosen parameter values are the same as for the high-spin states (Table 2,  $J = 0.863 \text{ eV}$ ) with the only exceptions being  $10Dq$  and  $\Delta_{\text{eff}}$ , which were treated as variable parameters. A diagram analogous to Fig. 9a but accounting for mixing between the  $d^5$ ,  $d^6L$ , and  $d^7L^2$  multiplets due to hybridization using values of  $T_e$  and  $T_i$  from Table 2 (0.7 and 1.4 eV, respectively) is plotted in Fig. 9b. In the following, the  $d^7L^2$  configuration will be neglected for reasons of simplicity; however, its effect on the calculations and the phase separation lines (Fig. 9b) was accounted for. A spin-orbit energy diagram representing all the necessary spin configurations for  $d^5$ ,  $d^6L$ , their zero-order energies and mixing via hybridization is depicted in Fig. 10. In Fig. 10 we have shown the  ${}^6A_1$  high-spin ( $S = 5/2$ ), the  ${}^4T_1$  intermediate-spin ( $S = 3/2$ ), and the  ${}^2T_2$  low-spin ( $S = 1/2$ ) states of  $d^5$  with their charge transfer states of  $t_2$  and  $e$  symmetry. The other intermediate spin state,  ${}^4T_2$ , is found to be at about  $1500 \text{ cm}^{-1}$  higher energy than  ${}^4T_1$  due to a less favorable Coulomb exchange (see above). The  ${}^6A_1$  ( $d^5$ ) state hybridizes with the ligand hole states of  $t_2$  symmetry, which have an  $e^2t_2^4$  configuration on metal. This state is  $10Dq$  higher in energy compared to the normal high-spin  $e^3t_2^3$  state resulting from the  $d^6e(L)$  configuration. The low-spin  ${}^2T_2$  ( $d^5$ ) hybridizes with a  $d^6t_2(L)$  state, which has the intermediate spin configuration  $e^4t_2^2$ . The intermediate spin  ${}^4T_1$  ( $d^5$ ) state hybridizes with a  $d^6t_2(L)$  state, which has a high-spin  $e^3t_2^3$  configuration on the metal. As follows from Fig. 10, both the high-spin  $d^6e(L)$  and the intermediate-spin  $d^6t_2(L)$  charge transfer states are favored by the crystal field, in contrast to the high-spin  $d^6t_2(L)$ , which is  $10Dq$  higher in energy. Double-hole, charge transfer states yield a minor contribution to the ground state energy (as long as  $U_{\text{eff}}$  is much larger than  $\Delta_{\text{eff}}$ ) but they stabilize mainly the low-spin state. It should be noted that without hybridization the high-spin  $d^5$  ( ${}^6A_1$ ) and the  $d^6L$  ( ${}^4T_1$ ) ground states are the only alternatives as long as  $10Dq < 3J$  and the low-spin  $d^5$  ground state is not stabilized. In this case it is the high-spin state  ${}^6A_1$  which is most stable when  $10Dq$  is larger than  $\Delta_{\text{eff}}$ ; otherwise ( $\Delta_{\text{eff}} < 10Dq$ ) the intermediate-spin state becomes most stable as long as the  $t_2-e$  splitting of the ligand levels ( $\delta W$ ) takes nonzero values. The latter increases the energy of the  $d^6e(L)$  high-spin state with respect to the  $d^6t_2(L)$  intermediate spin state (see Fig. 10). The  $S = 5/2 \rightarrow S = 1/2$  spin crossover for the  $d^5$  configuration, as predicted by the Tanabe–Sugano diagrams, may only occur when  $\Delta_{\text{eff}}$  becomes sufficiently large ( $\Delta_{\text{eff}} > 3J$ ); otherwise the  $S = 5/2$  and  $S = 1/2$   $d^5$  regions become separated by an intermediate  $S = 3/2$   $d^6L$  region. The mixing of  $d^5$  states with  $d^6L$  states due to hybridization



**FIG. 9.** Regions of stability for high- ( $S = 5/2$ ), low- ( $S = 1/2$ ), and intermediate-spin ( $S = 3/2$ ) ground states in isolated  $\text{FeS}_4^{2-}$  tetrahedra without ( $T_r = T_e = 0$ ) (a) and accounting for ( $T_r = 1.4$  eV,  $T_e = 0.7$  eV) (b)  $\text{Fe}(3d)\text{-S}(3s,3p)$  hybridization in dependence of the crystal field splitting parameter  $10Dq$  and the effective charge transfer energy  $\Delta_{\text{eff}}$ . The point approximately representing the ground state of  $\text{FeS}_4^{2-}$  in  $\text{Na}_3\text{FeS}_4$  is also indicated. Values of  $J$  and  $U_{\text{eff}}$  are 0.863 and 10.37 eV, respectively (see text and Table 3).

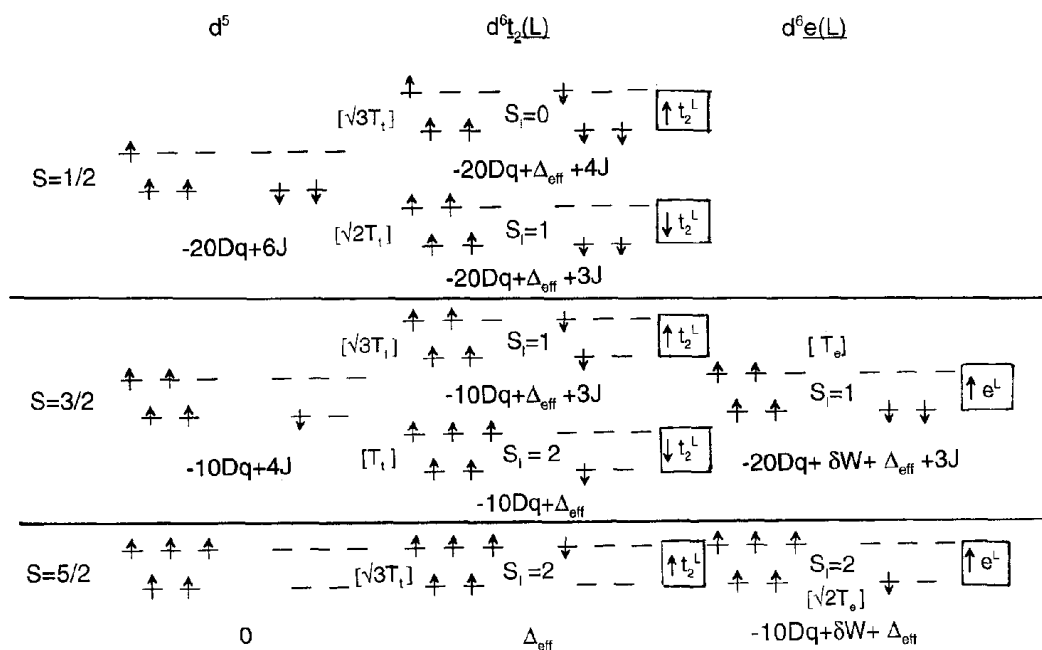


FIG. 10. Possible spin states for the ionic  $d^5$  and their counterparts from the corresponding singly ( $d^6L$ ) excited charge transfer configurations in tetrahedral symmetry.

( $T_i$  nonzero) is most pronounced for the high-spin  $S = 5/2$  ( $\sqrt{3}T_i$ ), followed by the low-spin  $S = 1/2$  ( $\sqrt{2}T_i$ ) and intermediate  $S = 3/2$  ( $T_i$ ) spin states which can be seen in Fig. 10. Comparing Figs. 9a and 9b, the high-spin stability region is larger and has shifted toward the lower  $\Delta_{\text{eff}}$  values due to the higher admixture of  $d^5$  character in the ground state. The low-spin-high-spin separation lines are moved correspondingly toward lower  $10Dq$  values, due to the increased exchange energy in the  $d^6L$  low-spin state (Fig. 10), which is of intermediate-spin character for  $d^6$ . For sufficiently low values of the parameter  $\Delta_{\text{eff}}$ , the drop of the  $d^6L$  high-spin state due to covalency and exchange stabilization from mixing with  $d^5$  is not enough to overcome the stabilization of the  $S = 3/2$  ( $d^6L$ ) state; as a result the intermediate spin-state region is achieved. The neglect of the splitting in the ligand levels  $\delta W$  leads to a narrowing of the intermediate state region, accompanied by a shift of the crossing point for the  $S = 5/2$ ,  $3/2$ , and  $1/2$  states toward lower values of  $\Delta_{\text{eff}}$ . Thus for the parameter range adopted in Fig. 9b the intermediate spin range disappears when taking  $\delta W = 0$ .

In Fig. 9b we also indicated the point which, according to the parameter set in (Table 3, high-spin parameters), represents the high-spin state of  $\text{FeS}_4^{5-}$  in  $\text{Na}_5\text{FeS}_4$ . This point is energetically well separated from the  $S = 3/2$  and  $S = 1/2$  stability ranges (cf. Table 5), in contrast with the  $S = 3/2$  ground state region where  $S = 1/2$  and  $S = 5/2$  excited states become quite close in energy. Therefore one hardly expects that ground states such as  $S = 3/2$  or  $S = 1/2$  for tetrahedrally coordinated  $\text{Fe}^{3+}$  may become stabi-

lized, using chemical manipulations leading to dimers or higher oligomers.

#### IV. CONCLUDING REMARKS

1. Experimental  $L$ -edge X-ray absorption spectra of  $\text{Na}_5\text{FeS}_4$  are well reproduced using atomic multiplet calculations in which covalency has been taken into account. The  $S = 5/2$  ground state deduced from this interpretation is in good agreement with optical and magnetic susceptibility data (7, 14). The XAS spectra on  $\text{KFeS}_2$  and a theoretical analysis strongly indicate that the  $\text{FeS}_4^{2-}$  tetrahedra are best described as being of high spin as well. Calculations of the ground state energies in dependence on the model parameters allow one to locate the  $\text{FeS}_4^{2-}$  ground state on a diagram with lines separating regions of stability for the possible  $S = 5/2$ ,  $3/2$ , and  $1/2$  ground states. The parameter values for  $\text{FeS}_4^{2-}$  in  $\text{Na}_5\text{FeS}_4$  ( $\Delta_{\text{eff}} = 0.68$  eV,  $10Dq = 0.5$  eV, and  $T_r = 1.4$  eV), deduced from a fit to the observed band profile, allow one to characterize the  $S = 5/2$  ground state as energetically well separated from the  $S = 1/2$  and  $S = 3/2$  states. Therefore, solid-state effects such as low symmetric ligand fields, which manifest themselves when going from separate to interconnected  $\text{FeS}_4^{2-}$  units, can hardly change the ground state to low ( $S = 1/2$ ) or intermediate ( $S = 3/2$ ) ground states, in contrast to octahedrally coordinated  $\text{Fe}^{3+}$  ions. In the latter cases, low-spin-high-spin equilibria are frequently encountered and a first example of an  $S = 3/2$  ground state (in  $\text{SrCoO}_3$ ) with negative  $\Delta$  have been also indicated (32). ESR data give further

support for the high-spin  $\text{Fe}^{3+}$ : the  $g$  value in  $\text{KFeS}_2$  ( $g = 2.03$  (33, 34)) is indeed very close to the spin-only value, showing (as expected for  $S = 5/2$ ) negligible orbital contributions. A high-spin ground state for  $\text{Fe}^{5+}$  is also indicated by the vanishingly small magnetic anisotropies reported from inelastic neutron scattering experiments on  $\text{KFeS}_2$  (34) and  $\text{TlFeS}_2$  (35) and  $X\alpha$  valence bond scattered wave calculations on  $\text{Fe}(\text{SR}_4)^{1-}$  and  $\text{FeS}_2(\text{SR}_4)^{2-}$  clusters ( $R = \text{H}, \text{CH}_3$ ) (14). In view of the high-spin configuration on  $\text{Fe}^{3+}$  a reinterpretation of the magnetic susceptibility data and neutron scattering experiments based on  $\text{TlFeS}_2$  ( $S = 3/2$ , (35)),  $\text{Na}_3\text{FeS}_3$  ( $S = 3/2$ , (16)), and  $\text{KFeS}_2$  ( $S = 1/2$ , (5, 15)) would be highly desirable. The unusually low-ordered moments seen in the neutron scattering and the very low magnetic hyperfine field from Mössbauer data (6) can be only partly explained by the small  $S$  to Fe charge transfer energy, which leads to an almost 1:1 admixture of  $d^5$  and  $d^6L$  functions in the ground state already in the separate  $\text{FeS}_4^{5-}$  units. Another important contribution might result from the partial compensation of up and down spin densities as well as from important contributions of the  $4s$  orbitals of iron.

The spin-densities on iron, [ $(3d) \uparrow 4.94$  ( $3d$ )  $\downarrow 1.11$  ( $4s$ )  $\uparrow 0.43$  ( $4s$ )  $\downarrow 0.42$ ], and the calculated hyperfine field of 250 kG (in good agreement with the magnitude of the experimental value 221 kG in  $\text{KFeS}_2$  (6)) as deduced from  $X\alpha$  calculations (13) are indeed quite compatible with a local high-spin state for Fe. In view of this, it should be noted that the rather low magnetic moments deduced from inelastic neutron scattering experiments may result from form-factor values considerably affected by covalency.

2. The main effects which result when going from  $\text{FeS}_4^{5-}$  to chains is the apparent lowering of symmetry around  $\text{Fe}^{3+}$  from almost  $T_d$  (separate  $\text{FeS}_4^{5-}$  units in  $\text{Na}_5\text{FeS}_4$ ) to  $D_{2d}$  ( $\text{KFeS}_2$ ). This is reflected by the strongly polarized absorption spectra (7) and quadrupolar splittings from Mössbauer data (6). Strong polarization effects due to S–S intrachain interactions are also indicated by some anisotropic Van Vleck susceptibilities in the chain compound  $\text{TlFeS}_2$  (35). A calculation on an  $\text{FeS}_8^{16-}$  cluster which accounts for ligand–ligand overlap shows that the symmetry lowering around  $\text{Fe}^{3+}$  is accompanied by a shift of the  $d$  orbitals to higher energies, which is particularly pronounced for the  $MO$  orbital of  $3d_{z^2}$  type. This is drawn here as an explanation for the broadening of the XAS profile to higher energies from  $\text{Na}_5\text{FeS}_4$  to  $\text{KFeS}_2$ . Dipolar magnetic fields due to the symmetry lowering may serve another contribution to the rather suppressed magnetic moments reflected by the Mössbauer data.

3. The parameter values derived from the X-ray absorption data show a strong intermixing of multiplets originating from the  $d^5$  and  $d^6L$  configurations. It is found that the  ${}^6A_1$  and  ${}^4T_1$ ,  ${}^4T_2$ , and  ${}^2T_2$  originating from the  $d^5$  con-

figuration are involved in a different coupling to corresponding states of  $d^6L$  of the same spin and symmetry. The resulting bonding and/or Coulomb repulsion effects differ from one multiplet to another. For such systems ligand-field (crystal field or angular overlap model) interpretations of optical data (such as given in Ref. (7)) are found not to be applicable because they make use of sets of one- and two-electron quantities which are approximated as common for all  $d^5$  multiplets.

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